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Functional Phases and Angular Momentum Characteristics of Tkatchev and Kovacs

Running Title: Tkatchev and Kovacs on high bar

Key words: Biomechanics, Coaching, Men’s Gymnastics, High Bar

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27

Abstract

28 Understanding the technical requirements and underlying biomechanics of complex release and
29 re-grasp skills on high bar allows coaches and scientists to develop safe and effective training
30 programmes. The aim of this study was to examine the differences in the functional phases
31 between the Tkatchev and Kovacs skills and to explain how the angular momentum demands
32 are addressed. Images of 18 gymnasts performing 10 Tkatchevs and [8](#) Kovacs at the Olympic
33 Games were recorded (50_Hz), digitised and reconstructed (3D Direct Linear Transformation).
34 Orientation of the functional phase (FP) action, defined by the rapid flexion to extension of the
35 shoulders and extension to flexion of the hips as the performer passed through the lower
36 vertical, along with shoulder and hip angular kinematics, angular momentum and key release
37 parameters (body angle, mass centre velocity and angular momentum about the mass centre
38 and bar) were compared between skills. Expected differences in the release parameters of
39 angle, angular momentum and velocity were observed and highlighted the specific mechanical
40 requirement of each skill. Whilst there were no differences in joint kinematics, hip and shoulder
41 FP were significantly earlier in the circle for the Tkatchev. These findings highlight the
42 importance of the orientation of the FP in the preceding [giant swing](#) and provides coaches with
43 further understanding of the critical timing in this key phase.

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47 **Introduction**

48 Complex release and re-grasp skills on high bar provide male artistic gymnasts with the
49 opportunity to maximise scoring potential. In men's gymnastics of the many release
50 skills the two most commonly performed are the Tkatchev and Kovacs (Samuels et al.,
51 2009), as detailed in the Fédération Internationale de Gymnastique (FIG) code of points
52 (2013 Tkatchev page 140, Kovacs page 143).

53 Body segment orientation during the aerial phase (e.g. straddled, tucked, and straight)
54 determines the difficulty rating of each skill (FIG, 2013). Previous research has reported
55 angular momentum profiles and release characteristics associated with successful
56 performance of each of these skills (Arampatzis and Brüggemann, 1999, 2001; Hiley et
57 al., 2007; Irwin et al., 2007). These studies have also shown that accelerated giant
58 swings are used to create the necessary release characteristics (Arampatzis and
59 Brüggemann, 1999, 2001; Hiley et al., 2007). The accelerated giant swing has been
60 previously split into the 'traditional' and 'scooped' (Hiley et al., 2007) or 'conventional'
61 and 'power' (Arampatzis and Brüggemann, 2001) techniques; however, research
62 investigating both techniques has agreed on the fundamental contribution of the hip and
63 shoulder joint actions. Yeadon and Hiley (2000) explained that the gymnast is
64 attempting to create a positive balance between the angular momentum gained in the
65 descent and lost in the ascending phase. Irwin and Kerwin (2006) showed that the
66 positive balance is achieved through hyper flexion of the shoulders and hyperextension
67 of the hips followed by a rapid extension of the shoulders and flexion of the hips as they
68 passed the lower vertical and that 70% of the work done occurred during this lower
69 phase. Irwin and Kerwin (2005) referred to these actions as the *functional phases* (hips

70 and shoulders) and highlighted them as key to the development and ultimately to the
71 successful performance of the giant swing and more so for the one preceding release.

72 The formal evaluation of this skill is performed by qualified judges and is based on the
73 technique requirements dictated by the FIG (2013) which shows the movement patterns
74 and body positions used by judges to evaluate successful performance. Coaching
75 instruction and feedback focuses attention on extension and flexion at the hips and
76 shoulders all of which are dependant upon the specific requirements of the skill. The
77 interesting feature of these two skills is that the mass centre trajectories in the flight
78 phase are similar but their respective flight angular momenta are opposite in direction.
79 The gymnast is thus faced with the challenge of creating the release characteristics,
80 which will enable him to fly backwards over the high bar, but in the Tkatchev he has the
81 added challenge of reversing the direction of his angular momentum vector as he
82 approaches release.

83 Based on these key technical requirements and the underlying biomechanics of the
84 Tkatchev and Kovacs, the aim of this study was to examine the differences in the
85 functional phases between these two skills and to explain how the angular momentum
86 demands are addressed. Ecological validity and coaching relevance were maintained
87 through the analysis of data from Olympic Competition.

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91 **Method**

92 **Data collection:** The data for this study were collected during the 2000 Sydney
93 Olympic Games as part of the **International Olympic Committee Research Project where**
94 **ethical approval was obtained from the Federation of International Gymnastics and**
95 **University Ethical Committee.** Two camcorders (Sony Digital Handycam DCR VX1000E,
96 Japan) were positioned on one side of the bar approximately 35 m away from and 8 m
97 above the high bar. The optical axes of the cameras intersected at approximately 66°
98 over the centre of the high bar. Both cameras captured the images at 50 Hz with a
99 shutter speed of 1/600 s. Prior to the performances, images were recorded of a three
100 dimensional calibration matrix comprising 40 known points encompassing the apparatus
101 (5.2 m x 6 m x 3 m) (Figure [1](#)). During the competition, images of the straight Tkatchev
102 (n=10) and Kovacs (tucked, n=[4](#); straight, n=4) were recorded. The inclusion criterion
103 was based on the highest scoring gymnasts from the [competition](#). The 10 straight
104 Tkatchev's were selected based on the FIG judging criterion, **with the 10 performances**
105 **that were scored highest by different gymnasts being selected for analysis.** A set of
106 Kovacs was also selected, which included [4](#) tucked and 4 straight. An analysis of the 2
107 versions of the Kovacs demonstrated no difference in the key variables; as such the
108 Kovacs were pooled giving a match set ([Table 1](#)).

109 The FIG difficulty rating of these skills at the time of data collection was Kovacs tucked
110 = D; Kovacs piked or stretched = E, Tkatchev stretched = D. In total data from 18
111 gymnasts with masses and heights ([60.1 ± 4.72 kg and 1.65 ± 0.04 m](#)) included.

112 -----INSERT FIGURE [1](#) HERE-----

113 Images of the calibration object and gymnast performing the preceding [giant swing](#)
114 (from 20 fields preceding handstand to 20 fields post catch) and Tkatchev and Kovacs
115 were digitised using the TARGET [\(v1.1, APEX, Loughborough, UK\)](#) high resolution
116 motion analysis system (Kerwin, 1995). The centre of the high bar and the gymnast's
117 head, and his right and left wrists, elbows, shoulders, hips, knees, ankles, and toes
118 were digitised. A 12 parameter direct linear transformation (Marzan and Karara, 1975)
119 was implemented to calibrate the cameras and reconstruct the coordinate data. The
120 inertia parameters of each segment were customised using Yeadon's inertia model
121 (1990), limb lengths determined from the video analyses and each gymnast's height
122 and mass. Accuracy and reliability were established through repeated digitisations of
123 six spherical markers (0.10 m in diameter) at known locations within the calibrated
124 volume and digitised on different days.

125

126

127 **Data analysis:** The 3D coordinate data were processed with the 'ksmooth' function
128 (Mathcad¹⁴™, Adept Scientific, UK) with the parameter 's' set to 0.10. This routine has
129 similar characteristics to a Butterworth low-pass digital filter with the cut-off frequency
130 set to 4.5 Hz, (Kerwin and Irwin, 2006). The left and right sides of the body were
131 averaged to produce a four segment planar representation of the gymnast, (arm, trunk,
132 thigh and shank). The instants of release and re-grasp were defined by quantifying 'grip
133 radius' as the linear separation between the 'mid-wrists' and the centre of the high bar.
134 Release was considered to have occurred once the grip radius exceeded 10% more

135 than the maximum value obtained during the preceding giant swing. The angular
136 position of the gymnast about the bar was defined by the mass centre to neutral bar
137 location. In order to compare within and between gymnasts all data were interpolated in
138 1° intervals throughout the circle angle using a cubic spline function, (Mathcad¹⁴™). A
139 circle angle was defined as 90° when the gymnast was in a handstand position and
140 continued to 450° as he returned to handstand. The previously defined 'functional
141 phases' (Irwin and Kerwin, 2005) were used, with the start and end points described by
142 maximum hip extension to flexion and maximum shoulder flexion to extension for the
143 Kovacs. Due to the fact that the Tkatchev ended with the gymnast performing a hyper
144 flexion of the shoulder and hyperextension of the hips a third phase was also included in
145 this analysis. In order to accurately locate the start and end points of these phases, the
146 zero crossing points in the hip and shoulder angular velocity time histories were used
147 for each gymnast. Circle angles for the gymnast at the start (Event 1), middle (Event 2)
148 and end (Event 3) of the functional phases for the shoulders and hips for each Tkatchev
149 were calculated. When the third phase angular velocity of the joints did not reach zero
150 prior to release the gymnast's circle angle at release was reported. Lines joining the
151 elbow, shoulder and hip defined the relative shoulder angle (θ_s) with the corresponding
152 hip (θ_h) defined by lines joining the shoulder, hip and knee. Shoulder and hip angles
153 were defined as zero with the gymnast in a handstand position. Positive angles were
154 defined as extension at the shoulders and flexion at the hips. Linear velocity time
155 histories for the whole body CM in the horizontal (V_h) and vertical (V_v) direction were
156 calculated.

157 Joint angles and changes in joint angles at the shoulders and hips for each functional
158 phase were determined. Differentiation of linear and angular quantities was achieved
159 using a variation of Ridder's divided difference method (Press *et al.*, 1992). The phases
160 of the Tkatchev and Kovacs that were compared are illustrated in Figure [2](#).

161

162 -----INSERT FIGURE [2](#) HERE-----

163

164 Angular momentum about the gymnast's mass centre (L_c) and about the bar (L_b) were
165 calculated. Angular momentum of the gymnast represented as a point mass was
166 determined by $L_b = m_s \cdot r \cdot V_R$ where m_s is equal to the mass of the body, r is the vector
167 between the mass centre and the bar and V_R is the resultant linear velocity of the mass
168 centre of the body. L_c was calculated using; $L_c = \sum I_s \cdot \omega_s + m_s \cdot r^2 \cdot \omega_c$, where I_s is the
169 segment's moment of inertia about a transverse axis through its mass centre and ω_s is
170 the angular velocity of the segment [about it's mass centre](#) and ω_c is the angular velocity
171 of the segment about the mass centre of the body. To account for gymnasts of varying
172 size, angular momentum values were normalised (L_n) by dividing by the product of 2π
173 and the moment of inertia in a theoretical straight body position (anatomical [position](#)
174 with arm angle fully flexed), measured in straight somersaults per second (SS/s).
175 Absolute and normalised moment of inertia were also reported. All variables included in
176 the analysis are based on the underlying theoretical relationship that they have with
177 successful performance. Successful performance was defined as those gymnasts that
178 executed the skill following the guides lines of the FIG ([2013](#))

179 *Statistical Intervention*

180 Following tests for normality differences between the Kovacs groups (straight versus
181 tucked) and differences in discrete variables between Tkatchevs and the Kovacs were
182 quantified using independent 't' - tests with the alpha level (critical P value) set to a
183 conservative 0.01. To establish the meaningfulness of these data, effect size was also
184 reported as a d score (Cohen, 1988) and interpreted using Hopkins (2000) complete
185 scale (≤ 0.2 trivial, 0.2–0.6 small, 0.6–1.2 moderate, 1.2–2.0 large, 2.0–4.0 very large
186 and ≥ 4.0 perfect).

187
188 **Results**

189 Reconstruction accuracy was found to be similar to other video based analyses of gymnastics
190 conducted within the laboratory at 5 mm. Measurement accuracy based on repeated
191 digitizations of six known points within the calibrated volume was 6.5 mm with the
192 corresponding reliability for a single digitization of ~0.1% of the field of view in all three
193 dimensions. Initial comparison between tucked and straight versions of the Kovacs
194 showed no significant differences and in general small effect sizes for any of the key
195 variables associated with successful performance (Table 1); as such both data sets for
196 the Kovacs were pooled. Therefore results presented here quantify the differences
197 between the 'straight' Tkatchev and pooled 'tucked and straight' Kovacs.

198
199 -----INSERT TABLE 1 HERE-----

200 *Release Characteristics*

201 Six of the nine key release parameters associated with successful performance of these
202 skills showed a significant difference $P < 0.01$ (Table 2) with a general trend for moderate

203 effect sizes. The Tkatchev and Kovacs skill requires the gymnasts' mass centre to travel
204 backward over the bar, and for this sample of gymnasts the horizontal component of
205 that velocity was not different between the two skills. In contrast the vertical velocity was
206 significantly higher for the Kovacs compared to the Tkatchev ($P < 0.01$), which was
207 concurrent with a significantly lower release angle for the Kovacs.

208

209 -----INSERT TABLE 2 HERE-----

210 Differences in the biomechanical parameters at release that dictate the trajectory of the
211 mass centre are highlighted in Figure 3. The average peak height was greatest for the
212 Kovacs due to greater vertical velocity at release, and associated flight time,
213 compensating for lower release angle. The timing of the peak height also differed
214 between these two skills, specifically, the Tkatchev's peak height occurred before the
215 gymnast passed over the bar compared to the peak height in the Kovacs being directly
216 over the high bar (Figure 4).

217

218 -----INSERT FIGURE 4 HERE-----

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221 The technical requirements of the Tkatchev and Kovacs dictates that the polarity of the
222 angular momentum about the gymnast mass centre (L_{nc}) is opposite at release,
223 however angular momentum about the bar represented as a point mass (L_{nb})
224 demonstrated little difference between the two skills (Table 2). Interestingly even though
225 L_{nb} was not different, the release characteristics that contributed to L_{nb} showed

226 significant differences and moderate effect sizes (Table 2). Specifically, the vertical
227 velocity of the mass centre at release was significantly lower during the Tkatchev, due
228 in part to the higher angle of release. The gymnasts' moments of inertia at release were
229 not significantly different in the Tkatchev. Which may explain the similarities in Lnb, due
230 to the fact that this is an the homogenous population, i.e. the gymnasts' body masses
231 were similar and hence the radial separation of the mass centre from the bar was also
232 consistent across the two skills (Table 2).

233

234 *Functional Phases*

235 Significant differences and moderate effect sizes were observed between the Tkatchev
236 and Kovacs for the start and end positions of the shoulder and hip functional phases
237 (Table 3). The Tkatchev is characterised by earlier start and end positions compared to
238 the Kovacs, however similarities between both skills were observed for the change in
239 circle angle during the hip functional phase (Table 3, Figure 4).

240 -----INSERT FIGURE 4 HERE-----

241

242 -----INSERT TABLE 3 HERE-----

243

244 Shoulder flexion angles, at the start of the functional phase, were significantly greater
245 for the Tkatchev compared to the Kovacs, highlighting a more open shoulder position
246 when the Tkatchev skill is initiated (Table 4 and illustrated in Figure 2). The maximum
247 angular velocity of the shoulders was similar for both skills; however due to the post

248 functional phase actions required in the Tkatchev, a more dynamic hip action was
249 observed with a significantly greater maximum angular velocity of the hips.

250 -----INSERT TABLE 4 HERE-----

251

252 *Angular Momentum*

253 The angular momentum profile shown in Figure 5 demonstrates an increase in angular
254 momentum about the mass centre (L_{nc}) as the performer descends from handstand. As
255 anticipated, the reversal of angular momentum begins early in the preparatory swing
256 and has a greater rate of change, thus allowing the gymnast to begin reversing his
257 angular momentum after 80% of the swing phase.

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259 -----INSERT FIGURE 5 HERE-----

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263 Due to the specific needs of the Tkatchev (reversing the angular momentum to allow the
264 gymnast to rotate forwards in flight) there is a clear polarity change in L_{nc} before the
265 release point. In order to facilitate this reversal of angular momentum the gymnast
266 performs extra hip and shoulder actions, which are reflected in the differences in the
267 functional phase characteristics (Table 4).

268

269 The peak normalised angular momentum about the mass centre is similar for the
270 Kovacs and Tkatchev ($L_{nc} \approx 1.4$), but the L_{nc} reduction in the Kovacs is minimised to
271 ensure sufficient angular momentum at release to achieve the required backward
272 rotation in flight. L_{nc} for the Tkatchev changes from a peak of 1.4 to -0.5 at release,
273 enabling the gymnast to rotate forwards as he travels backwards over the bar.

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277 **Discussion**

278

279 The aim of this study was to examine the differences in the biomechanics of functional
280 phases between the Tkatchev and Kovacs and to explain how the angular momentum
281 demands of these complex release and re-grasp skills are addressed. Employing
282 biomechanical analyses, understanding of how the performer achieves the technical
283 requirements of these skills, as outlined by the international governing body, has been
284 developed. In addition examining the similarities between the preceding giant swing
285 provides useful information for coaching and scientists about skill development and
286 training methodology.

287 The data were checked for accuracy and reliability and values concurrent with other
288 similar studies were found (Kerwin and Irwin, 2010). The authors advocate the use of
289 data collected at international competition to provide insight into performances, although
290 the number of trials is low, the performances have high ecological validity and as such
291 can ultimately underpin our understanding.

292 It is clear from a coaching and performance perspective that the technical requirements
293 of these skills (Tkatchev and Kovacs) are different. Previous research by Brüggemann
294 *et al.*, 1994 classified these two skills as Category I (in which the direction of the angular
295 momentum is maintained) and Category II (in which the direction of the angular
296 momentum is changed prior to release). These authors identified a need to understand
297 and explain the mechanical demands underpinning the individual requirements of the
298 movements. Gaining insight into the technical requirements of these skills, particularly
299 at release and during the preceding [giant swing](#), will allow coaches and scientists to
300 better understand how gymnastics organise their body segments to achieve these skills
301 (Brüggemann *et al.*, 1994).

302 At release, differences were observed between these two skills for the majority of
303 release parameters (Table 2). The release parameters ensure the gymnast possesses
304 sufficient angular momentum to somersault as required by the particular skill and to
305 achieve a flight profile that guarantees a safe clearance and effective re-grasp of the bar
306 (Figure [3](#)). The Kovacs released earlier and achieved a greater peak height compared
307 to the Tkatchevs highlighted in Table 2. These differences result in a different trajectory,
308 in flight, for each skill as highlighted in Figure [3](#). In comparison to the data presented
309 previously, for the Kovacs, (Arampatzis and Brüggemann, 1999) and the Tkatchev
310 (Arampatzis and Brüggemann, 2001), the current study reported similar horizontal
311 release [velocities](#) (Table 5). [The angular momentum about the mass centre at release](#)
312 [was 19 and 27% higher in the current study for the Tkatchev and Kovacs, respectively](#)
313 [compared to the earlier data of Arampatzis and Brüggemann \(1999, 2001\), a finding](#)
314 [that may suggest a progressive evolution of these skills between 1994 and 2000 as the](#)

315 straight body version become the more popular. However, normalized data were not
316 available and this should be considered in the interpretation of these findings, although
317 the difference in the height and mass of the subjects was less than 3% and 1%
318 respectively.

319 -----INSERT TABLE 5 HERE-----

320 The importance of the giant swing preceding the Tkatchev and Kovacs was highlighted
321 by the earlier work of Brüggemann et al. (1994). These authors identified changes in the
322 joint angular kinematics due to the direct relationship that these have on the production
323 of angular momentum about the bar and about the mass centre for the subsequent
324 aerial phase. Building on earlier research in which Irwin and Kerwin (2005, 2006)
325 introduced the term “*functional phases*” to describe and explain the actions of the hips
326 and shoulders, observations from the current study highlight differences in the
327 orientation of the start and end points of the functional phases in the circle between the
328 two release and re-grasp skills. The functional phases of the Tkatchev start and finish
329 significantly earlier for the hips and shoulders (Figure 4, Table 3). The importance of this
330 finding rests with the development of these skills and the coach’s understanding of the
331 location of the key functional phases in the circle and how this changes as a function of
332 the skill requirements. The reversal of angular momentum prior to release necessary for
333 the Tkatchev highlights the need for developmental drills and progressions to replicate
334 the spatial and temporal characteristics of these actions to allow the appropriate
335 bio-physical adaptations to occur in the most effective and safe fashion. With the
336 exception of the shoulder angle at the start of the Tkatchev, joint angles at the start and
337 end of these phases were generally similar between these two skills. These findings

338 concur with the classic training principle of specificity and overload and point towards
339 the existence of a skill specific [giant swing](#) that may be taught in parallel, rather than in
340 series which is the current practice, which may facilitate a more effective skill
341 development programme.

342 **Conclusion**

343 The difference between the technical requirements of these skills is diverse and is
344 clearly evident due to the opposite polarity of the angular momentum at release.
345 However, with this in mind, the current study has highlighted that these complex skills
346 share a similar joint angular kinematic requirement during the functional phases,
347 although the orientation of these phases shift as a function of the type of skill. The
348 Tkatchevs functional phases started earlier and finished earlier compared to the
349 Kovacs. This information may lead to the development of skill specific [giant swings](#) that
350 can be used to elicit the specific requirements of these skills. The outcome of this would
351 be a more effective and safe training environment.

352

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410 **Acknowledgements**

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412 **Tables**

413

414 **Table 1.** Average (\pm sd) release characteristics for the tucked and straight Kovacs

	TUCK	STRAIGHT			
	KOVACS	KOVACS			
n	4	4	df	p	ES
θ_c	375.50	364.50	8	P>0.05 0.09	0.58
<u>sd</u>	5.07	9.81			
vCy	-1.64	-1.64	8	P>0.05 1.00	0.00
<u>sd</u>	0.25	0.08			
vCz	4.50	5.05	8	P>0.05 0.06	0.64
<u>sd</u>	0.10	0.46			
Lnc	1.00	0.82	8	P>0.05 0.07	0.65
<u>sd</u>	0.10	0.11			
Lnb	3.30	3.65	8	P>0.05 0.26	0.43
<u>sd</u>	0.10	0.51			
tFlight	1.00	0.98	8	P>0.05 0.41	0.21
<u>sd</u>	0.03	0.06			
ω_c	6.80	5.84	8	P>0.05 0.07	0.62
<u>sd</u>	0.30	0.80			
lcm	11.00	9.93	8	P>0.05 0.37	0.34
<u>sd</u>	1.30	1.65			
Incm	9.90	8.65	8	P>0.05 0.15	0.52
<u>sd</u>	1.30	0.67			

415 θ_c = angle of release ($^\circ$). vCy and vCz = velocity of the mass centre horizontally and vertically (m/s). Ln = normalised angular
416 momentum about the mass centre (c) and bar (b) (SS/s). tFlight = flight time (s). ω_c = angular velocity about the mass centre
417 (rad/s). lcm = moment of inertia about the mass centre (kgm^2), Incm = normalised moment of inertia.

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Table 2. Average (\pm sd) release characteristics for the Tkatchev and Kovacs

	TKATCHEV	KOVACS		
n	10	8	p	ES
θ_c	406.30	370.00	P<0.01	0.91
sd	6.72	9.32		
v_{Cy}	-1.78	-1.64	P>0.01	0.27
sd	0.31	0.17	0.27	
v_{Cz}	2.70	4.78	P<0.01	0.91
sd	0.53	0.42		
Lnc	-0.51	0.89	P<0.01	0.99
sd	0.08	0.12		
Lnb	3.28	3.49	P>0.01	0.25
sd	0.44	0.38	0.30	
tFlight	0.62	0.97	P<0.01	0.95
sd	0.06	0.05		
ω_c	-2.71	6.29	P<0.01	0.99
sd	0.50	0.74		
lcm	12.37	10.45	P>0.01	0.54
sd	1.48	1.49	0.02	
lncm	1.19	1.01	P>0.01	0.54
sd	0.14	0.14	0.02	

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θ_c = angle of release ($^\circ$). v_{Cy} and v_{Cz} = velocity of the mass centre horizontally and vertically (m/s). Ln = normalised angular momentum about the mass centre (c) and bar (b) (SS/s). tFlight = flight time (s). ω_c = angular velocity about the mass centre (rad/s). lcm = moment of inertia about the mass centre (kgm^2), lncm = normalised moment of inertia.

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Table 3. Average (\pm s) Circle angle (θ_c) for the start (s) and end (e) of the functional phases for the hips (H) and shoulders (S) during the Tkatchev and Kovacs

n	TKATCHEV	KOVACS	P	ES
	10	10		
θ_{cHs}	217	<u>269</u>	P<0.01	0.94
<u>sd</u>	12	<u>6</u>		
θ_{cHe}	314	<u>371</u>	P<0.01	<u>0.90</u>
<u>sd</u>	17	10		
θ_{cSs}	226	<u>284</u>	P<0.01	0.95
<u>sd</u>	12	7		
θ_{cSe}	347	<u>368</u>	P<0.01	<u>0.50</u>
<u>sd</u>	22	13		
$\Delta\theta_{cH}$	97	<u>101</u>	P>0.01	<u>0.22</u>
<u>sd</u>	9	9		
$\Delta\theta_{cS}$	121	<u>84</u>	P<0.01	<u>0.81</u>
<u>sd</u>	15	12		

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θ = angle (degrees)

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Table 4 Average (\pm sd) joint kinematics at the start (s) and end (e) of the functional phases for the hips (H) and shoulders (S) during the Tkatchev and Kovacs

	TKATCHEV	KOVACS	P	ES
θ Hs	-39.5	<u>-31.8</u>	P>0.01	0. <u>50</u>
sd	8.3	<u>4.4</u>	<u>0.03</u>	
θ He	54.9	<u>59.3</u>	P>0.01	0. <u>22</u>
sd	6.5	<u>12.0</u>	<u>0.33</u>	
θ Ss	-16.5	<u>-6.0</u>	P<0.01	0. <u>79</u>
sd	4.8	<u>3.1</u>		
θ Se	42.3	<u>50.1</u>	P>0.01	0. <u>44</u>
sd	7.9	<u>7.9</u>	<u>0.05</u>	
min ω H	-8.0	-2.5	P<0.01	0. <u>98</u>
<u>sd</u>	0.7	0.4		
max ω H	9.8	<u>8.0</u>	P<0.01	0. <u>60</u>
<u>sd</u>	1.3	1.1		
min ω S	-9.5	-1.5	P<0.01	0.96
<u>sd</u>	1.7	<u>0.4</u>		
max ω S	4.4	<u>5.5</u>	P>0.01	0. <u>52</u>
<u>sd</u>	0.8	<u>1.00</u>	<u>0.02</u>	

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θ = angle (degrees)/ ω = angular velocity (Rad/s)

506 **Table 5.** Comparison of selected release characteristics (mean ±sd) from the current study and
 507 Arampatzis & Brüggemann (1999 and 2001)

	Arampatzis & Brüggemann (1999) 1994 World Championships "Kovacs"	Current Study 2000 Olympic Games "Kovacs"	Arampatzis & Brüggemann (2001) 1994 World Championships "Tkatchev"	Current Study 2000 Olympic Games "Tkatchev"
vCy	-1.60	-1.64	-1.97	-1.78
sd	0.34	0.17	0.38	0.31
vCz	4.76	4.78	3.06	2.70
sd	0.4	0.42	0.44	0.53
Lc	46.1	58.5	-33.39	-39.6
sd	2.7	11.7	4.55	5.43

508 vCy and vCz = velocity of the mass centre horizontally and vertically (m/s). Lc = angular momentum about the mass centre
 509 (kgm²/s).
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511 **Figures**

512

513 **Figure 1.** Graphical illustration of the dimensions of the men's high bar (above) three
514 dimensional calibration object (below)

515 **Figure 2.** Illustration of the functional phase (shoulder and hips combined) and release point
516 during the Tkatchev (above) and Kovacs (below) performed at the 2000 Olympic Games
517 Sydney

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519 **Figure 3.** Average mass centre trajectory during the flight phase (m) for the Tkatchev (Black)
520 and Kovacs (grey)

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522 **Figure 4.** Average shoulder (left) and hip (right) start and end points of the Functional Phases
523 for the Tkatchev (black) and Kovacs (grey)

524 **Figure 5.** Average (\pm s) Normalised angular momentum (SS/s) about the gymnasts mass centre
525 (Lnc) for the Tkatchev (black) and Kovacs (grey) from the start of the functional phase to
526 release performed at the 2000 Olympic Games Sydney.

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